

# Adapting learning models to distribution shifts with affine alignment

**Antoine Collas - CMAP Retreat 2025**  
**Inria Saclay - Mind team**



13/06/2025

1. **Introduction to Domain Adaptation (DA)**
2. **Skada-Bench: Benchmarking Unsupervised DA methods**
3. **Joint shifts in  $(X, y)$  on manifolds: GOPSA**

# 1. Introduction to Domain Adaptation (DA)

# Supervised learning

Independent and identically distributed data:

$$\{(x_n, y_n)\}_{n=1}^N \sim \mathbb{P}(X, Y)$$

$x_n \in \mathcal{X}$ , e.g.  $\mathbb{R}^d$  and  $y_n \in \mathcal{Y}$ , e.g.  $\{-1, 1\}$  for binary classification

Goal: find a predictor  $f: \mathcal{X} \mapsto \mathcal{Y}$  by **empirical risk minimization**

$$\min_{f \in \mathcal{F}} \left\{ \hat{R}(f) = \frac{1}{N} \sum_{n=1}^N \ell(y_n, f(x_n)) \right\}$$

with  $\ell$  a loss function

# Domain Adaptation (DA) Problem

Source domain ( $\mathcal{S}$ ) and Target domain ( $\mathcal{T}$ ) with

$$\mathbb{P}_{\mathcal{S}}(X, Y) \neq \mathbb{P}_{\mathcal{T}}(X, Y)$$

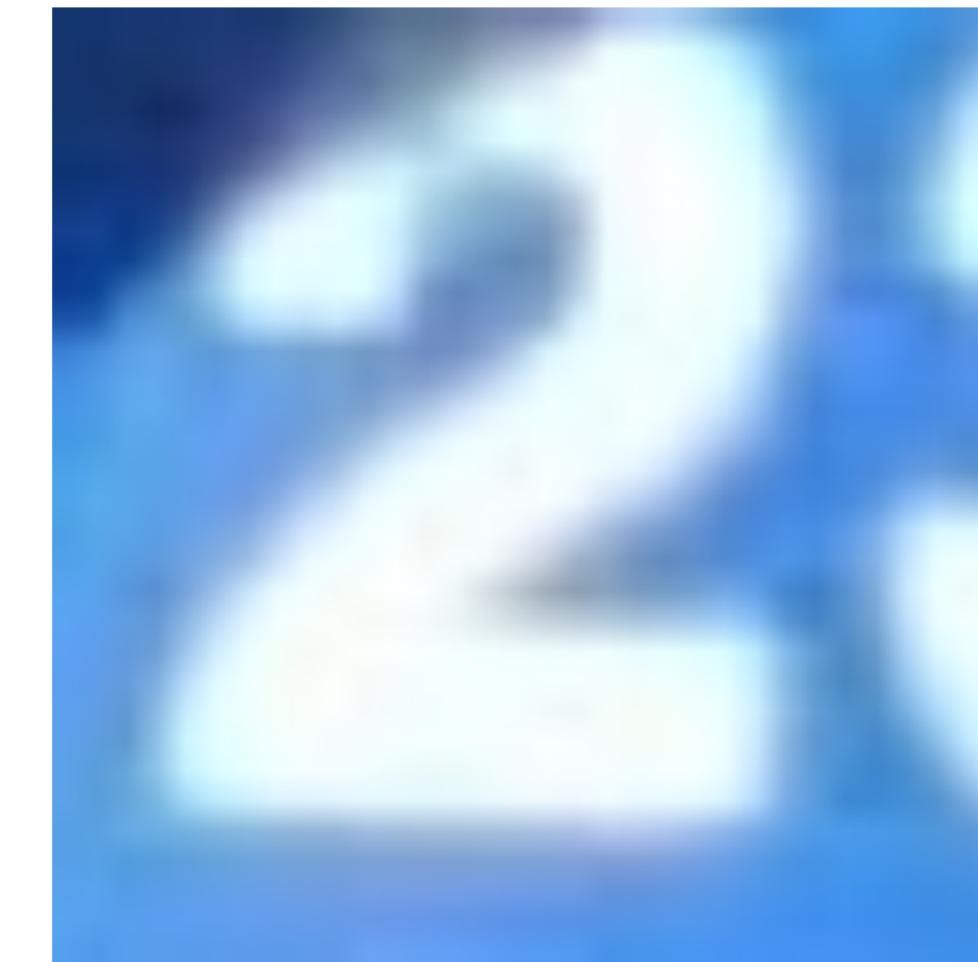
Source domain ( $\mathcal{S}$ ): MNIST



2

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Target domain ( $\mathcal{T}$ ): SVHN



2

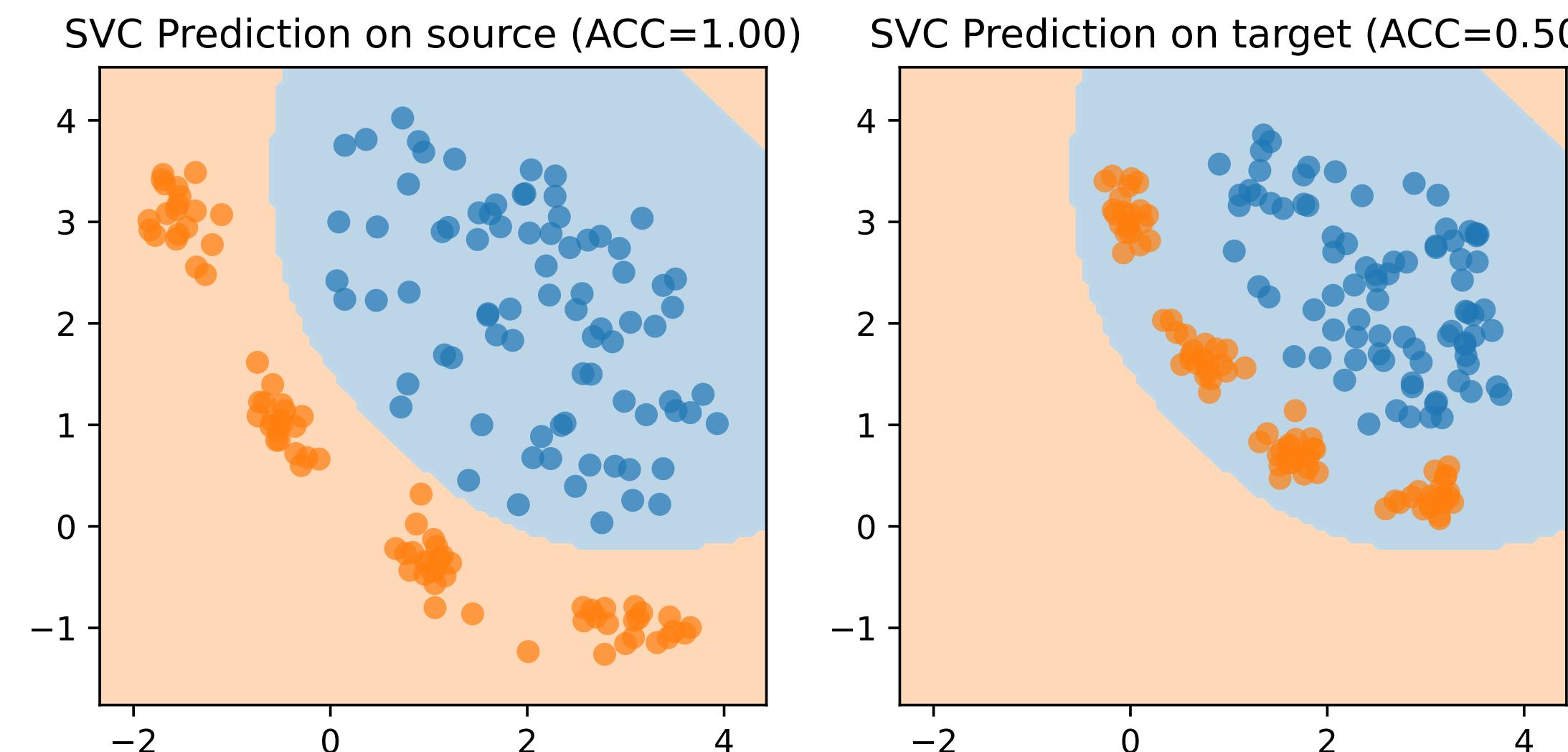
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# Domain Adaptation (DA) Problem

Source domain ( $\mathcal{S}$ ) and Target domain ( $\mathcal{T}$ ) with

$$\mathbb{P}_{\mathcal{S}}(X, Y) \neq \mathbb{P}_{\mathcal{T}}(X, Y)$$

Training on the source domain (classical empirical risk minimization):



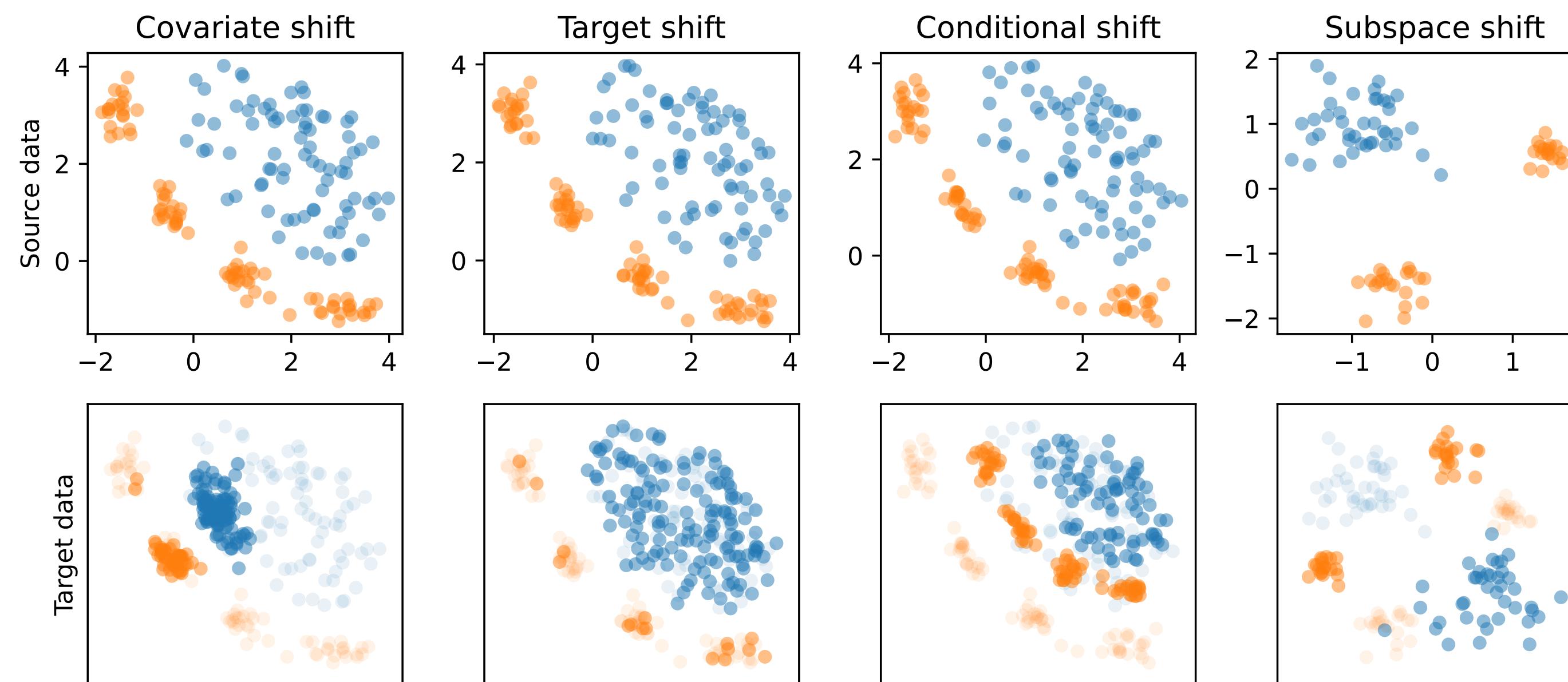
Simple shifts can lead to very bad classifications on the target domain!

# Unsupervised DA Problem

Source domain is labeled:  $\{(x_n, y_n)\}_{n=1}^{N^{\mathcal{S}}} \sim \mathbb{P}_{\mathcal{S}}(X, Y)$

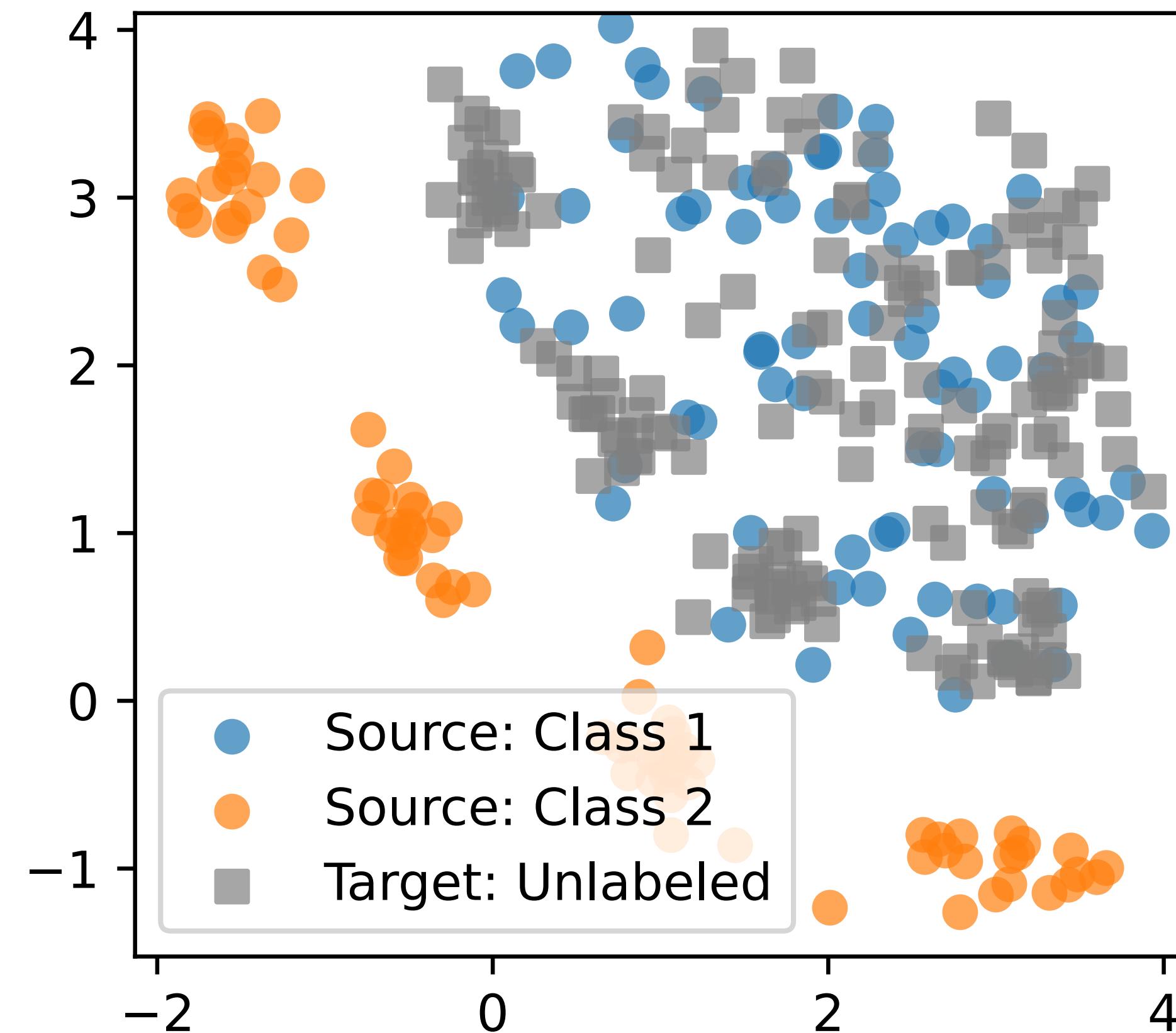
Target domain is unlabeled:  $\{(x_n, \cdot)\}_{n=1}^{N^{\mathcal{T}}} \sim \mathbb{P}_{\mathcal{T}}(X, Y)$

Assumptions on the shift between  $\mathbb{P}_{\mathcal{S}}(X, Y)$  and  $\mathbb{P}_{\mathcal{T}}(X, Y)$ :



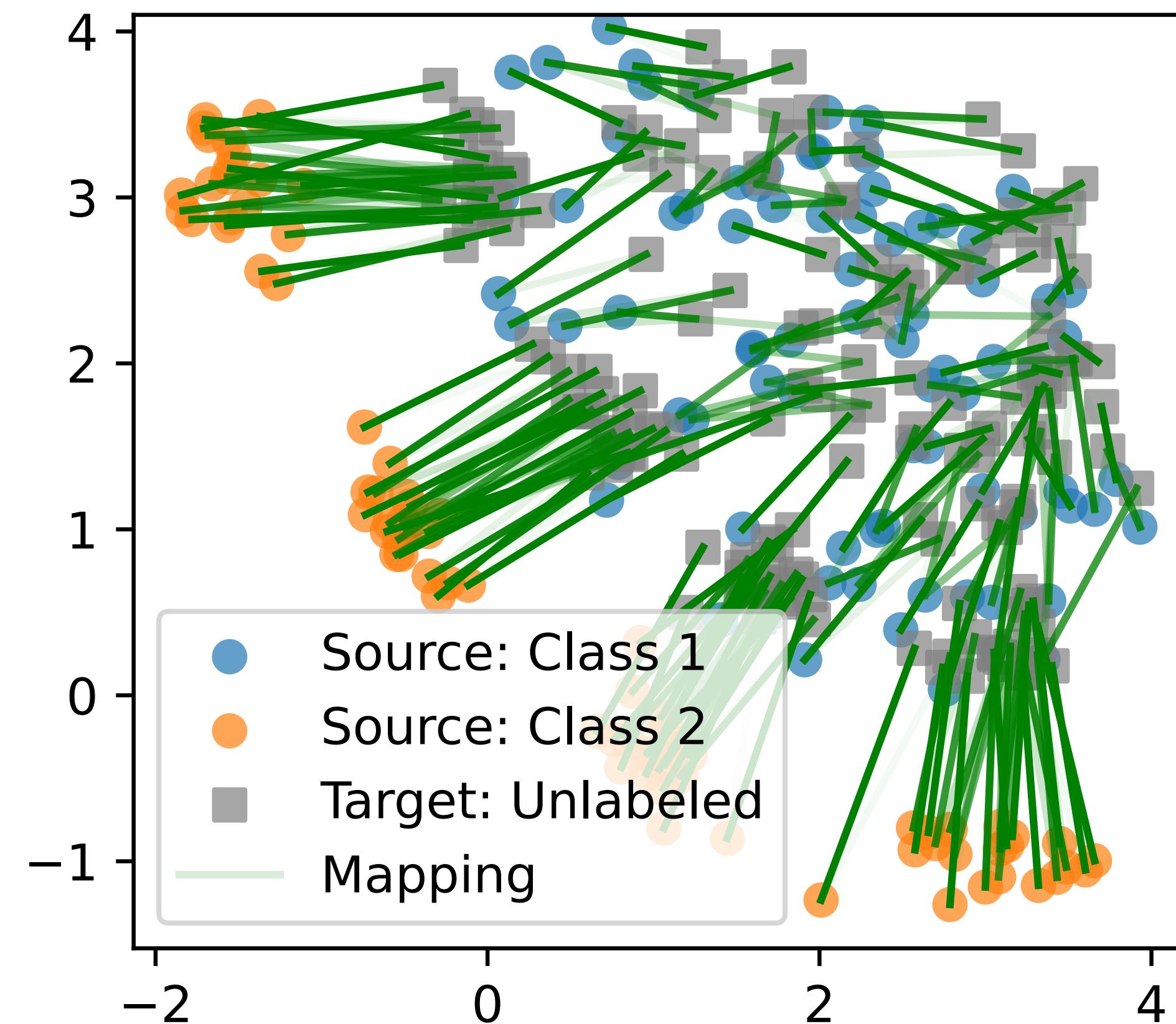
# Toy Example: Mapping-Based UDA

Problem setting:



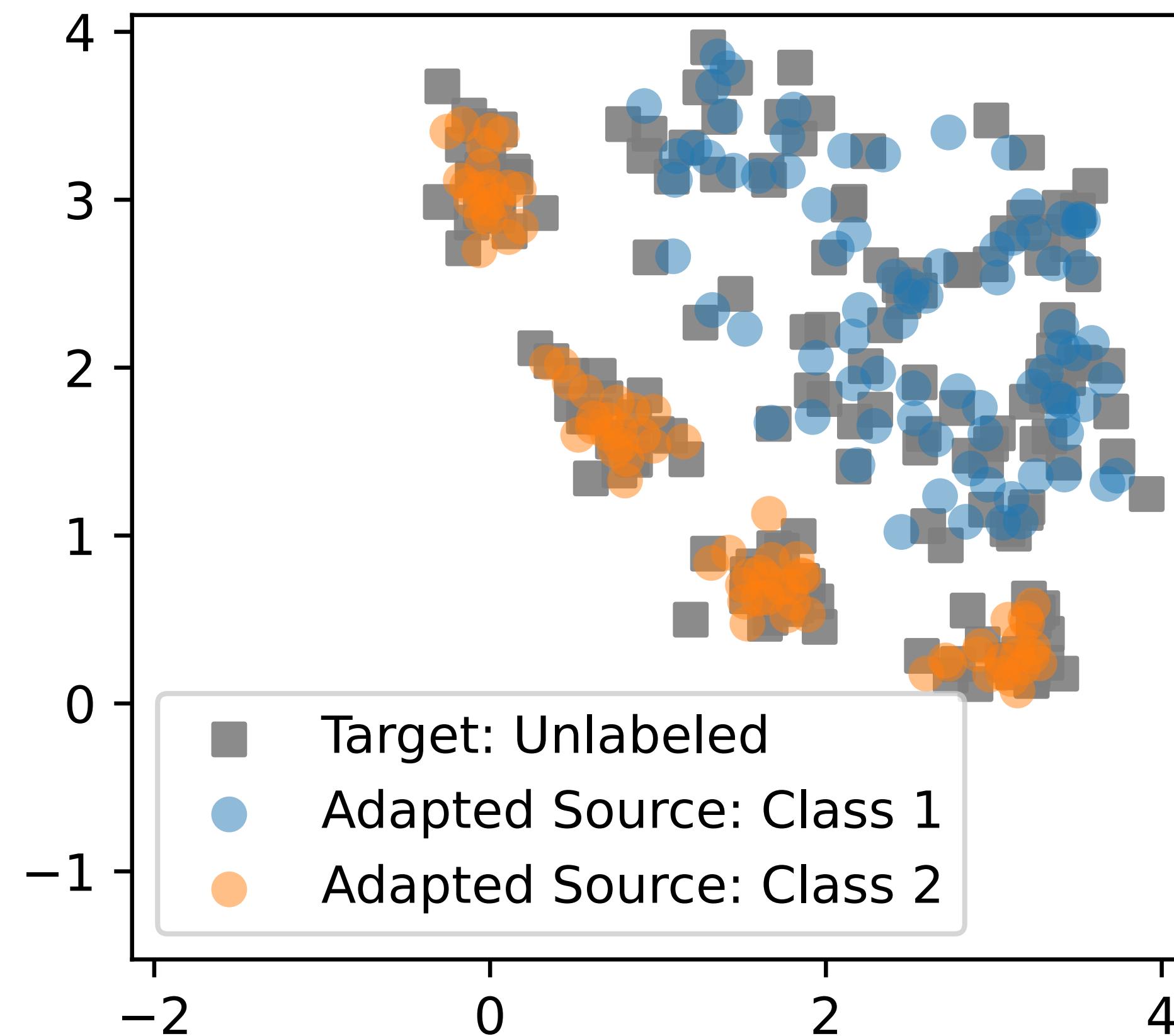
# Toy Example: Mapping-Based UDA

Mapping computation:



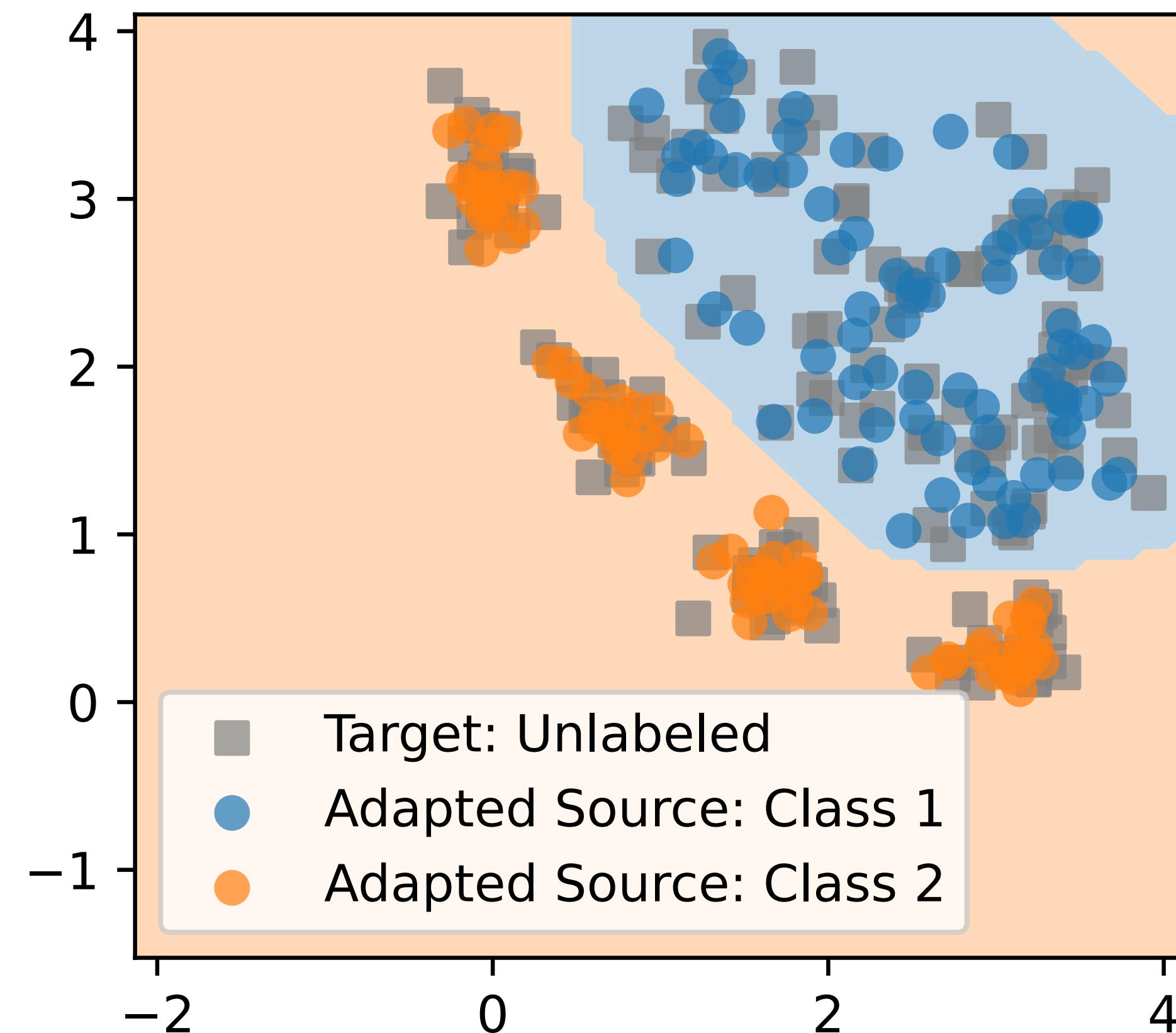
# Toy Example: Mapping-Based UDA

Mapping application:



# Toy Example: Mapping-Based UDA

Classifier fitting:



# DA methods

Mapping:

$$f_{\text{DA}} = f \circ m$$

where  $m$  aligns source and target domains

$m$  can be a normalization, subspace projection, optimal transport mapping, ...

Reweighting:

$$f_{\text{DA}} \in \arg \min_{f \in \mathcal{F}} \frac{1}{N_S} \sum_{n=1}^{N_S} w_i \ell(y_n, f(x_n))$$

where  $w_i$  are importance weights depending on source and target domains

End-to-End Deep Learning:

Adversarial or discrepancy losses to align source and target distributions

# Scikit-Adaptation: Skada

Python library for domain adaptation:

- Sklearn-like API with estimators (.fit, .predict, . . . ), pipeline, grid search
- Shallow and Deep learning methods
- DA scorers to validate hyper-parameters without using target labels



<https://github.com/scikit-adaptation/skada>



## 2. SKADA-Bench: Benchmarking Unsupervised DA methods

Yanis Lalou\*, Théo Gnassounou\*, AC\*, Antoine de Mathelin\*, Oleksii Kachaiev,  
Ambroise Odonnat, Alexandre Gramfort, Thomas Moreau, Rémi Flamary

\*Equal contribution

<https://arxiv.org/abs/2407.11676>

# Motivation and setup

Evaluate DA methods across diverse modalities:

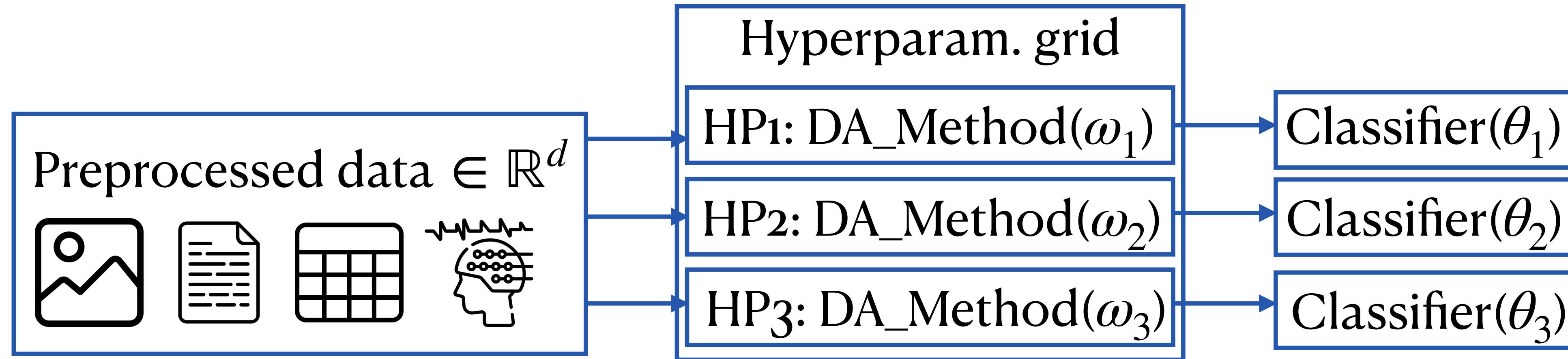
- 8 real-wold datasets of 4 modalities
- 4 synthetic datasets
- 51 adaptation pairs (source → target)
- 20 DA Methods
- 5-fold nested cross-validation
- built with Skada

Dataset	Modality	Preprocessing
Office 31	CV	Decaff + PCA
Office Home	CV	ResNet + PCA
MNIST/USPS	CV	Vect + PCA
20 Newsgroup	NLP	LLM + PCA
Amazon Review	NLP	LLM + PCA
Mushrooms	Tabular	One Hot Encoding
Phishing	Tabular	None
BCI	Biosignals	Cov + TS

<https://github.com/scikit-adaptation/skada-bench>

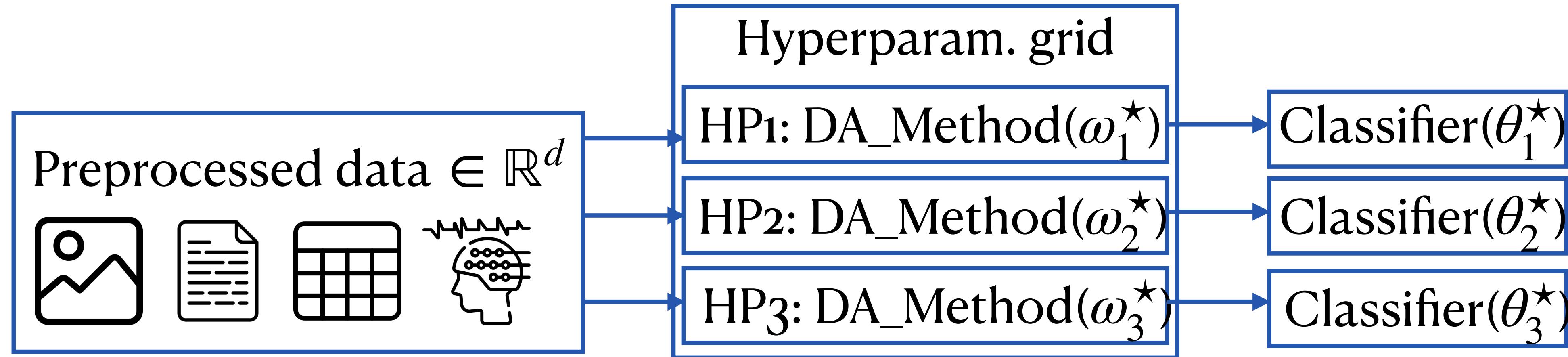
# Pipeline

- ① Training:  $(X_{\text{train}}^{\mathcal{S}}, y_{\text{train}}^{\mathcal{S}}, X_{\text{train}}^{\mathcal{T}})$



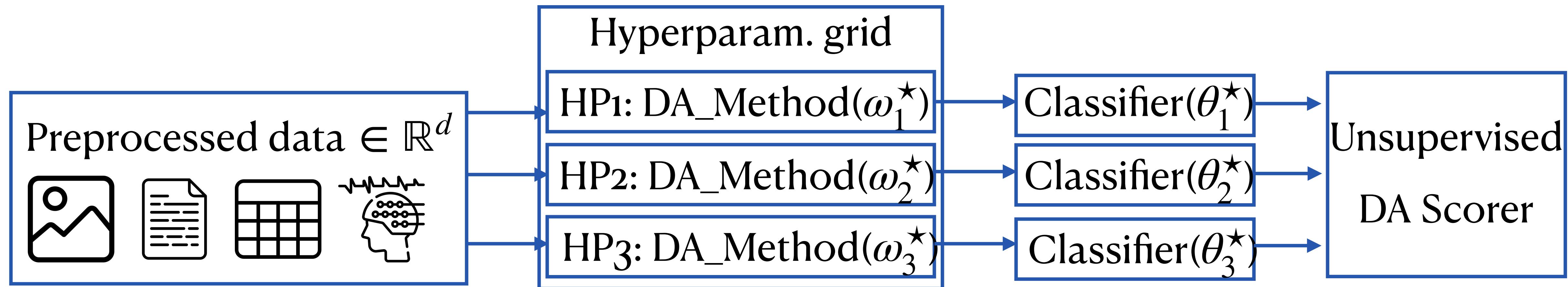
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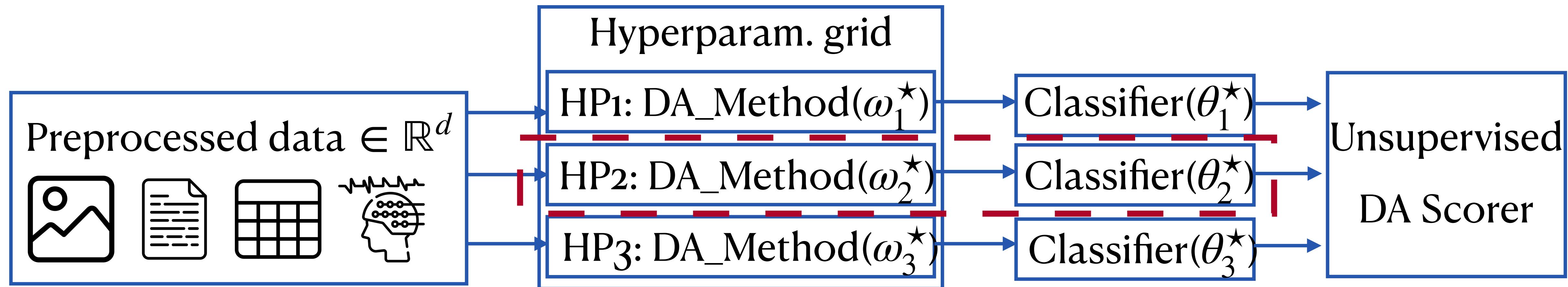
# Pipeline

- ② Validation:  $(X_{\text{val}}^{\mathcal{S}}, y_{\text{val}}^{\mathcal{S}}, X_{\text{val}}^{\mathcal{T}})$



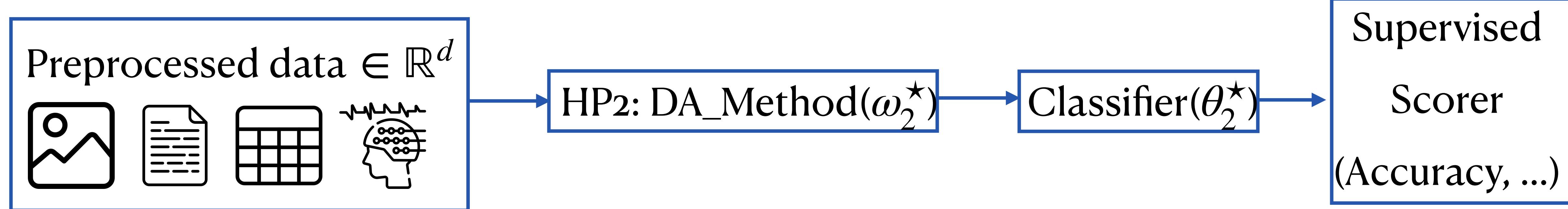
# Pipeline

- ② Validation:  $(X_{\text{val}}^{\mathcal{S}}, y_{\text{val}}^{\mathcal{S}}, X_{\text{val}}^{\mathcal{T}})$



# Pipeline

③ Evaluation:  $(X_{\text{test}}^{\mathcal{T}}, y_{\text{test}}^{\mathcal{T}})$



Realistic setup: no target labels for training, labels used only for benchmarking

# Results

## Synthetic

## Real

Adaptation

= gain  
 = loss

		Cov. shift	Tar. shift	Cond. shift	Sub. shift	Office31	OfficeHome	MNIST/USPS	20NewsGroups	AmazonReview	Mushrooms	Phishing	BCI	Selected Scorer	Rank
	Train Src	0.88	0.85	0.66	0.19	0.65	0.56	0.54	0.59	0.7	0.72	0.91	0.55		10.66
	Train Tgt	0.92	0.93	0.82	0.98	0.89	0.8	0.96	1.0	0.73	1.0	0.97	0.64		1.55
Reweighting	Dens. RW	0.88	0.86	0.66	0.18	0.62	0.56	0.54	0.58	0.7	0.71	0.91	0.55	IW	12.20
	Disc. RW	0.85	0.83	0.71	0.18	0.63	0.54	0.5	0.6	0.68	0.75	0.91	0.56	CircV	8.75
	Gauss. RW	0.89	0.86	0.65	0.21	0.22	0.44	0.11	0.54	0.55	0.51	0.46	0.25	CircV	16.45
	KLIEP	0.88	0.86	0.66	0.19	0.65	0.56	0.54	0.6	0.69	0.72	0.91	0.55	CircV	10.56
	KMM	0.89	0.85	0.64	0.16	0.64	0.54	0.52	0.7	0.57	0.74	0.91	0.52	CircV	11.74
	NN RW	0.89	0.86	0.67	0.15	0.65	0.55	0.54	0.59	0.66	0.71	0.91	0.54	CircV	9.15
	MMDTarS	0.88	0.86	0.64	0.2	0.6	0.56	0.54	0.59	0.7	0.74	0.91	0.55	IW	10.81
Mapping	CORAL	0.74	0.7	0.76	0.18	0.65	0.57	0.62	0.73	0.7	0.72	0.92	0.62	CircV	5.08
	MapOT	0.72	0.57	0.82	0.02	0.6	0.51	0.61	0.76	0.68	0.63	0.84	0.47	PE	10.21
	EntOT	0.71	0.6	0.82	0.12	0.64	0.58	0.6	0.83	0.62	0.75	0.86	0.54	CircV	9.40
	ClassRegOT	0.74	0.58	0.81	0.11	NA	0.53	0.62	0.97	0.68	0.82	0.89	0.52	IW	8.25
	LinOT	0.73	0.73	0.76	0.18	0.66	0.57	0.64	0.82	0.7	0.76	0.91	0.61	CircV	4.06
	MMD-LS	0.78	0.72	0.76	0.56	0.65	0.56	0.55	0.97	0.63	0.85	NA	0.5	MixVal	8.22
Subspace	JPCA	0.88	0.85	0.66	0.15	0.62	0.48	0.51	0.77	0.69	0.78	0.9	0.54	PE	8.98
	SA	0.74	0.68	0.8	0.11	0.65	0.57	0.56	0.88	0.67	0.78	0.89	0.53	CircV	7.80
	TCA	0.52	0.47	0.51	0.62	0.04	0.02	0.07	0.61	0.61	0.49	0.48	0.26	DEV	17.58
	TSL	0.88	0.85	0.66	0.2	0.63	0.48	0.45	0.63	0.69	0.45	0.89	0.26	IW	15.09
Other	JDOT	0.72	0.58	0.82	0.13	0.6	0.42	0.59	0.79	0.67	0.65	0.79	0.47	IW	11.42
	OTLabelProp	0.72	0.59	0.8	0.07	0.66	0.56	0.62	0.86	0.67	0.64	0.86	0.5	CircV	10.01
	DASVM	0.89	0.86	0.65	0.15	NA	NA	NA	0.87	NA	0.83	0.85	NA	MixVal	7.29

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= gain  
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	DASVM	0.89	0.86	0.65	0.15	NA	NA	NA	0.87	NA	0.83	0.85	NA	MixVal	7.29

# Affine Distribution Alignment Across Domains

CORAL (Correlation Alignment) [Sun et al., 2017]

Aligns second-order moments between source and target:

$$m(x) = \Sigma_{\mathcal{T}}^{\frac{1}{2}} \Sigma_{\mathcal{S}}^{-\frac{1}{2}} x, \quad \arg \min_A \|A \Sigma_{\mathcal{S}} A^\top - \Sigma_{\mathcal{T}}\|_F^2$$

LinOT (Linear Optimal Transport) [Flamary et al., 2019]

Affine map minimizing transport cost between  $\mathbb{P}_{\mathcal{S}} = \mathcal{N}(\mu_{\mathcal{S}}, \Sigma_{\mathcal{S}})$  and  $\mathbb{P}_{\mathcal{T}} = \mathcal{N}(\mu_{\mathcal{T}}, \Sigma_{\mathcal{T}})$ :

$$m(x) = Ax + b \quad \text{with} \quad A = \Sigma_{\mathcal{S}}^{-\frac{1}{2}} \left( \Sigma_{\mathcal{S}}^{\frac{1}{2}} \Sigma_{\mathcal{T}} \Sigma_{\mathcal{S}}^{\frac{1}{2}} \right)^{\frac{1}{2}} \Sigma_{\mathcal{S}}^{-\frac{1}{2}}, \quad b = \mu_{\mathcal{T}} - A\mu_{\mathcal{S}}$$

# Normalization Across Domains

Many **benefits**:

- easy to code
- fast
- no need to access source and target data simultaneously
- no/few hyperparameters
- unsupervised: no target labels required

# Normalization Across Domains

How to deal with ...?

- ...target shifts, i.e. joint shifts ( $X, y$ )?
- ...several source domains, i.e. multi-source adaptation?
- ... $\mathcal{X} = \mathcal{M}$ , i.e. data on manifolds?

# 3. Joint shifts in $(X, y)$ on manifolds: GOPSA

Apolline Mellot\*, AC\*, Sylvain Chevallier,  
Alexandre Gramfort, Denis A. Engemann

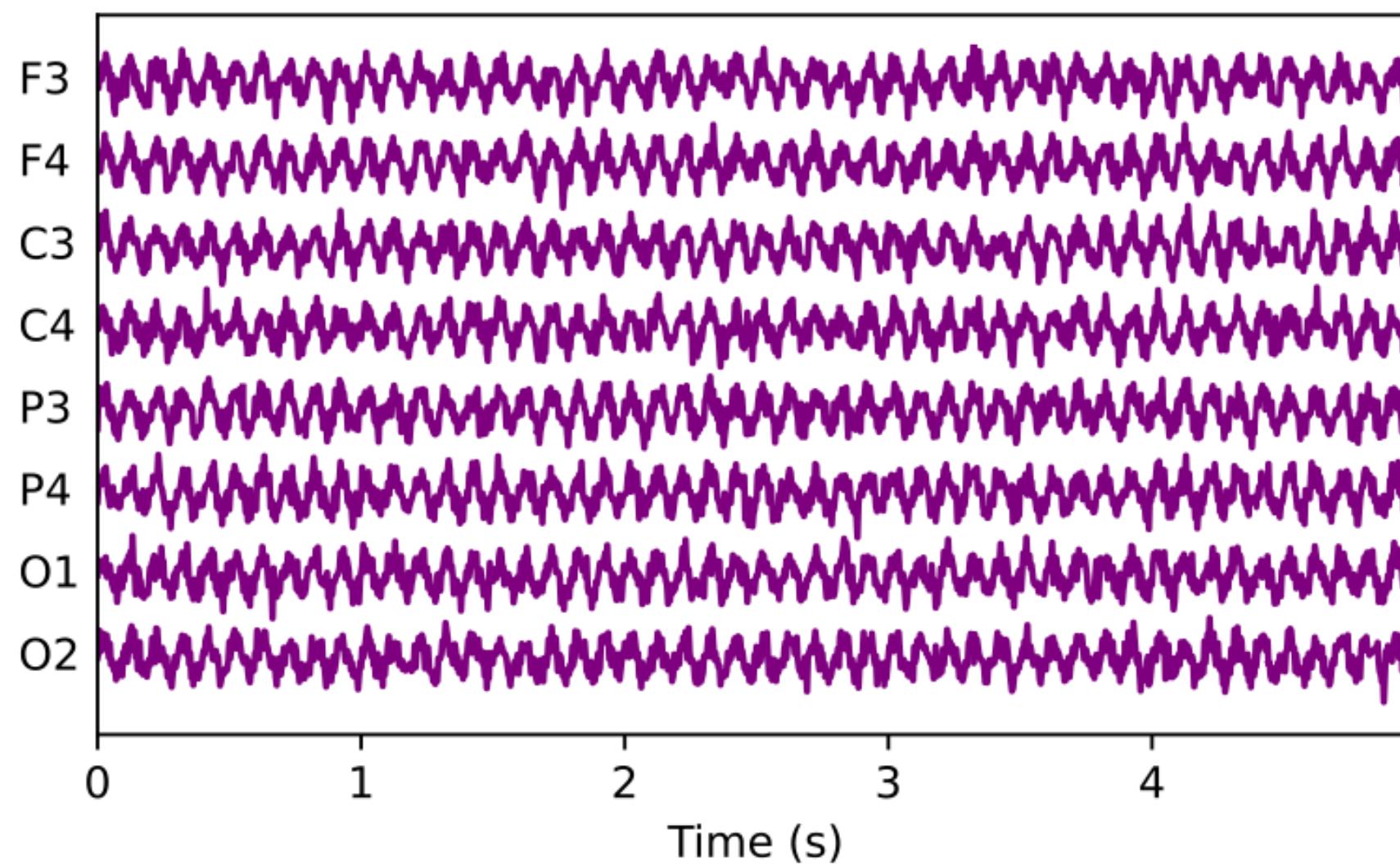
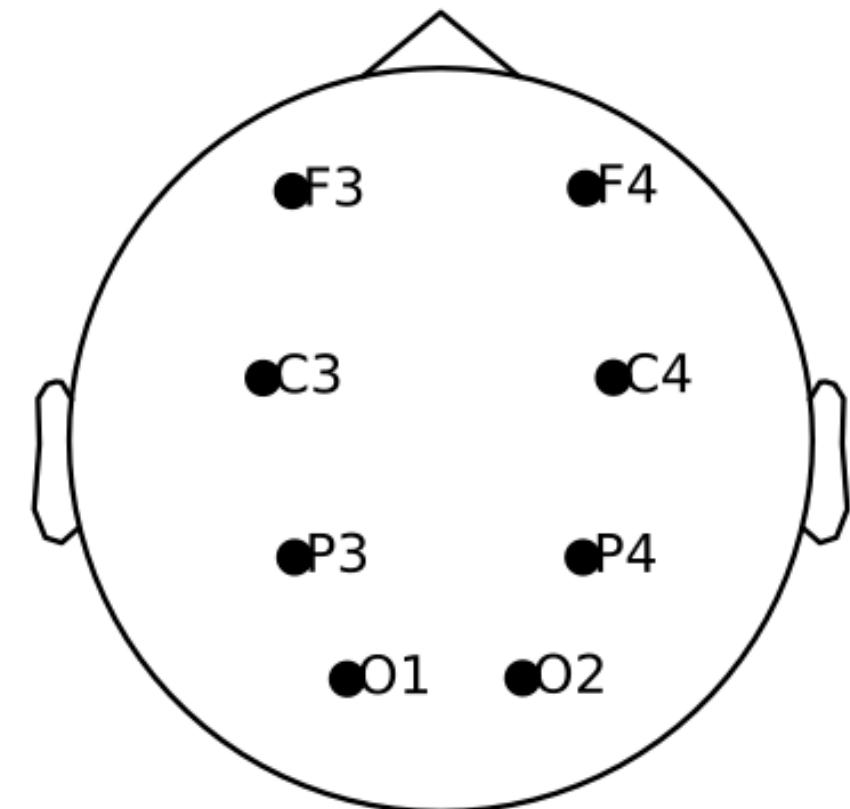
\*Equal contribution

NeurIPS 2024, Spotlight

<https://arxiv.org/abs/2407.03878>

# Machine learning on EEG data

Predicting an outcome from neural activity measured by EEG, a non-invasive technique that records brain signals from the scalp.

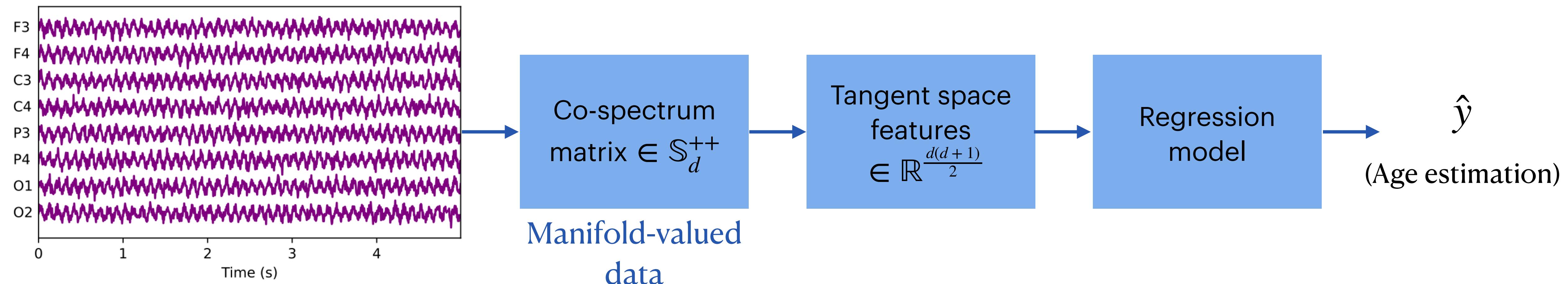


## Applications:

sleep staging (awake, deep sleep, ...), brain-computer interface, biomarker regression, ...

# Brain age: subject-level regression

1 time series = 1 subject



Brain age is a proxy for cognitive health and detects deviations from typical aging

# Co-spectrum

Let  $x_\ell \in \mathbb{R}^d$  be a stationary zero-mean time series

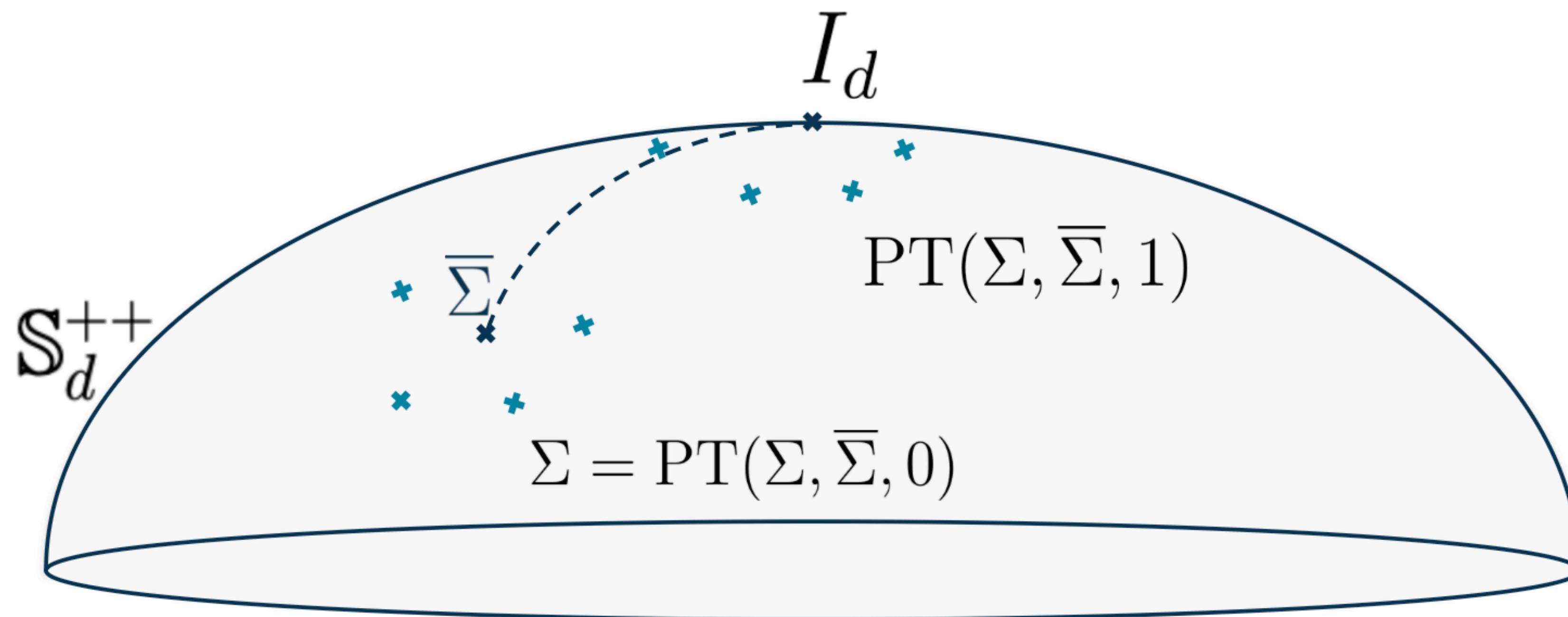
$$R(\tau) = \mathbb{E} [x_{\ell+\tau} x_\ell^\top] \in \mathbb{R}^{d \times d}$$

$$C(s) = \operatorname{Re} \left\{ \sum_{\tau=-\infty}^{\infty} e^{-i2\pi s\tau} R(\tau) \right\} \in \mathbb{S}_d^{++}$$

$[C(s_0), \dots, C(s_{F-1})]$  represents the time-series and belongs to the manifold  $(\mathbb{S}_d^{++})^F$

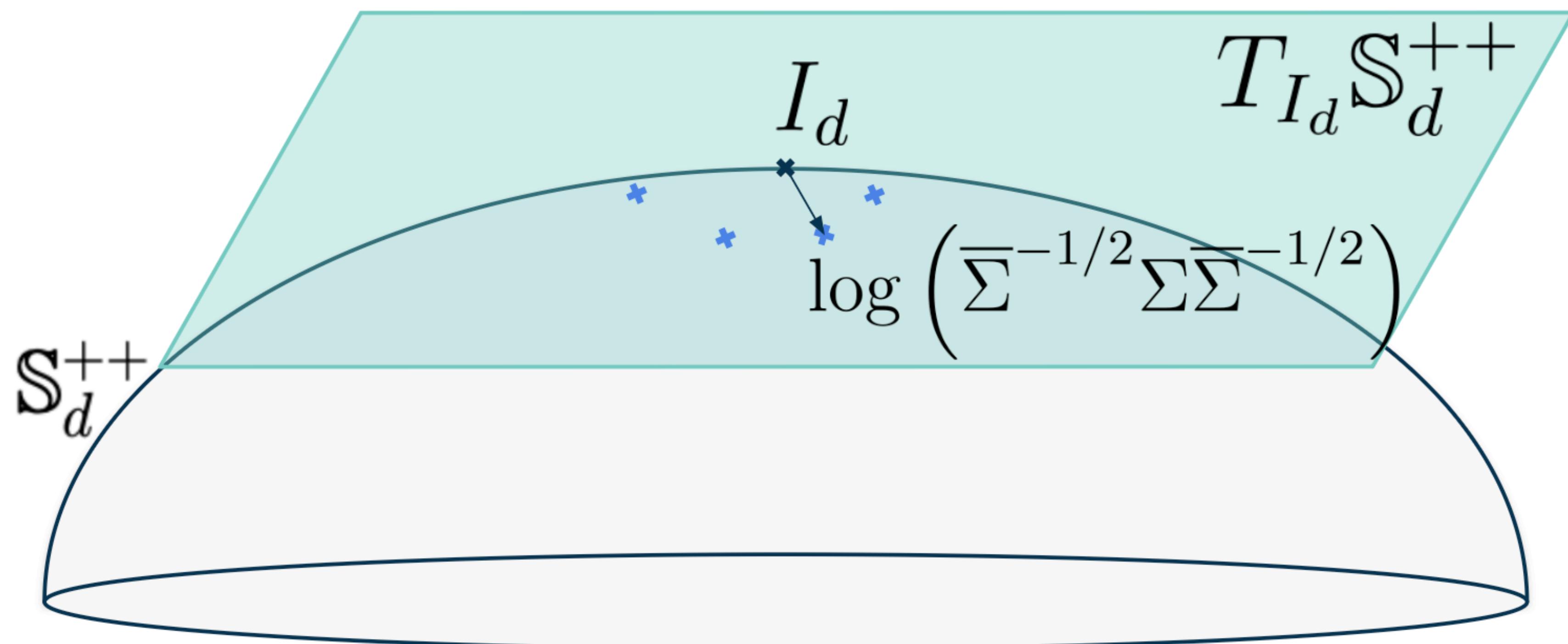
# Regression on $\mathcal{S}_d^{++}$

- ① Parallel transport moves  $\Sigma$  from  $\bar{\Sigma}$  to  $I_d$  at  $\alpha \in [0,1]$ :  $\text{PT}(\Sigma, \bar{\Sigma}, \alpha) = \bar{\Sigma}^{-\alpha/2} \Sigma \bar{\Sigma}^{-\alpha/2}$



# Regression on $\mathcal{S}_d^{++}$

- ② Riemannian logarithm of  $\Sigma$  at  $I_d$



# Regression on $\mathcal{S}_d^{++}$

③ Upper-triangular vectorization

$$\phi(\Sigma, \bar{\Sigma}) \triangleq \text{uvec}\left(\log\left(\bar{\Sigma}^{-1/2}\Sigma\bar{\Sigma}^{-1/2}\right)\right) \in \mathbb{R}^{d(d+1)/2}$$

④ Regression

$$\hat{y} = \beta^\top \phi(\Sigma, \bar{\Sigma})$$

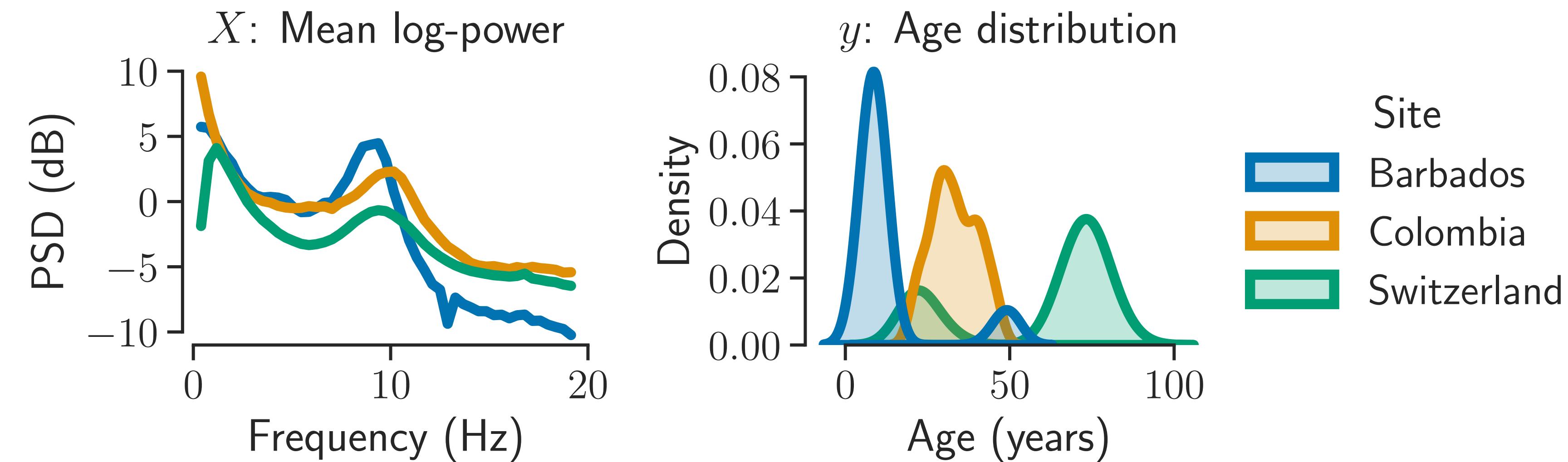
[Sabbagh, et al., 2019]

# Data shifts in neuroscience

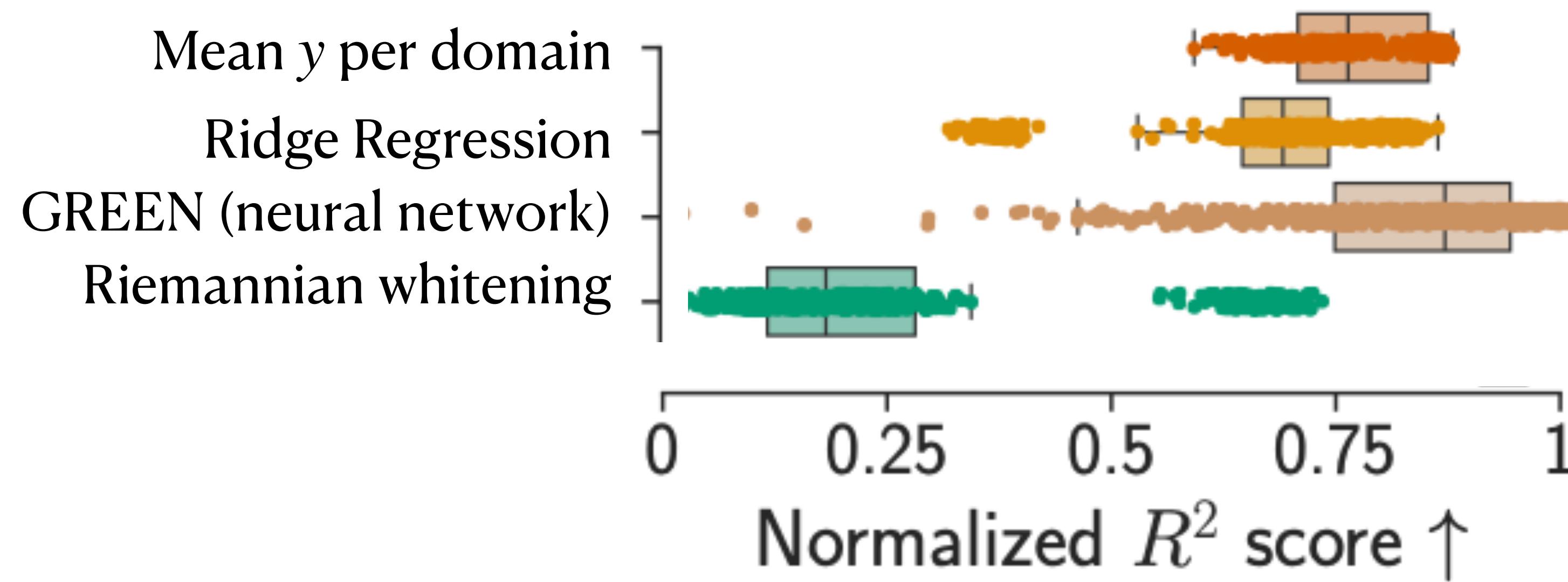
## Sources of variability:

- population: age, gender, diseased or healthy, ...
- hardware and preprocessing: sensors, positions, sampling rates, ...
- task-related variability: tasks during recording, level of engagement, external stimuli, ...

HarMNgEEG  
dataset  
[Li et al., 2022]



# Data shifts in neuroscience



# GOPSA: Geodesic Optimization for Predictive Shift Adaptation

**Setup:**

$K$  source domains:  $\{(\Sigma_{k,n}, y_{k,n})\}_{n=1}^{N_k}$  for  $k \in \{1, \dots, K\}$  and  $N_{\mathcal{S}} = \sum_{k=1}^K N_k$

One target domain:  $\{\Sigma_{\mathcal{T},n}\}_{n=1}^{N_{\mathcal{T}}}, \bar{y}_{\mathcal{T}}$  (mean value)

# GOPSA: Geodesic Optimization for Predictive Shift Adaptation

Setup:

$K$  source domains:  $\{(\Sigma_{k,n}, y_{k,n})\}_{n=1}^{N_k}$  for  $k \in \{1, \dots, K\}$  and  $N_{\mathcal{S}} = \sum_{k=1}^K N_k$

One target domain:  $\{\Sigma_{\mathcal{T},n}\}_{n=1}^{N_{\mathcal{T}}}, \bar{y}_{\mathcal{T}}$  (mean value)

Learn the parallel transport  $\alpha \in [0,1]$  per domain:

$$\phi(\Sigma, \bar{\Sigma}, \alpha) \triangleq \text{uvec} \left( \log_{I_d} (\text{PT}(\Sigma, \bar{\Sigma}, \alpha)) \right) = \text{uvec} \left( \log \left( \bar{\Sigma}^{-\alpha/2} \Sigma \bar{\Sigma}^{-\alpha/2} \right) \right)$$

# GOPSA: Geodesic Optimization for Predictive Shift Adaptation

Learnable source and target data matrices w.r.t.  $\alpha_{\mathcal{S}} \in [0,1]^K$  and  $\alpha_{\mathcal{T}}$ :

$$Z_{\mathcal{S}}(\alpha_{\mathcal{S}}) \triangleq \left[ \phi(\Sigma_{1,1}, \bar{\Sigma}_1, \alpha_1), \dots, \phi(\Sigma_{K,N_K}, \bar{\Sigma}_K, \alpha_K) \right]^\top \in \mathbb{R}^{N_{\mathcal{S}} \times d(d+1)/2}$$

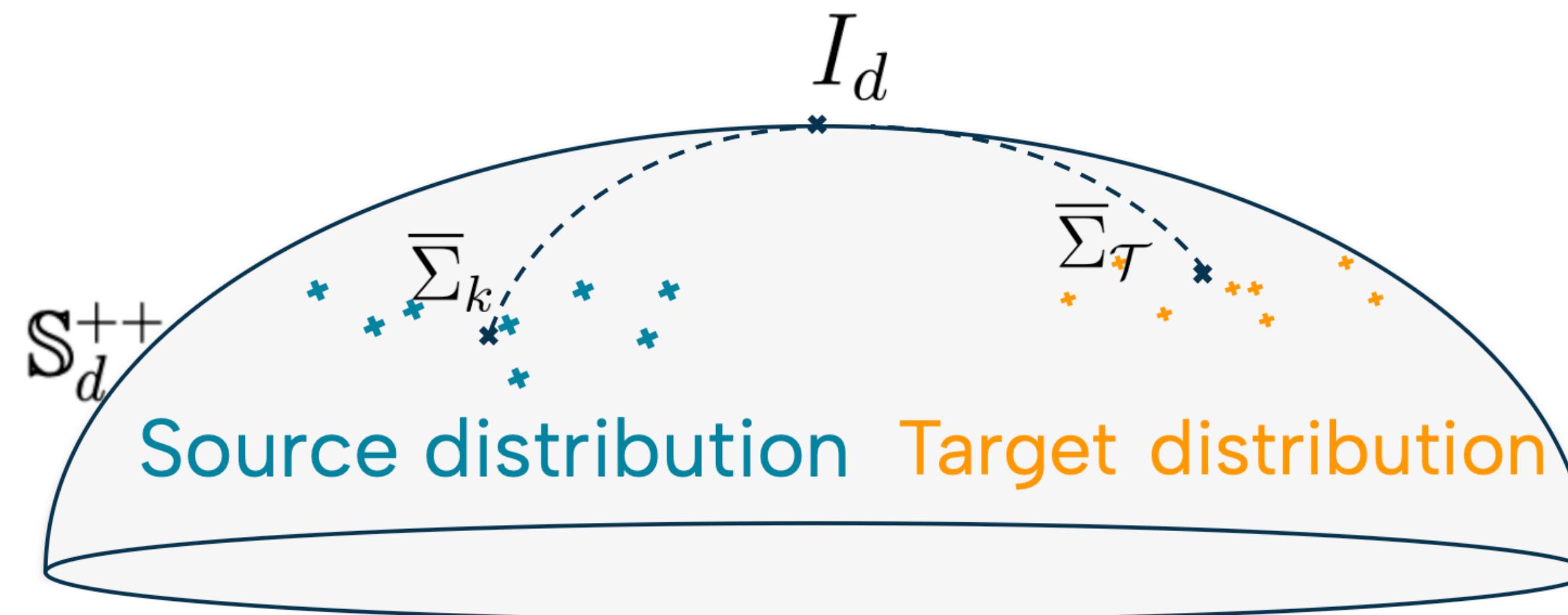
$$Z_{\mathcal{T}}(\alpha_{\mathcal{T}}) \triangleq \left[ \phi(\Sigma_{\mathcal{T},1}, \bar{\Sigma}_{\mathcal{T}}, \alpha_{\mathcal{T}}), \dots, \phi(\Sigma_{\mathcal{T},1}, \bar{\Sigma}_{\mathcal{T}}, \alpha_{\mathcal{T}}) \right]^\top \in \mathbb{R}^{N_{\mathcal{T}} \times d(d+1)/2}$$

# GOPSA: Geodesic Optimization for Predictive Shift Adaptation

Learnable source and target data matrices w.r.t.  $\alpha_{\mathcal{S}} \in [0,1]^K$  and  $\alpha_{\mathcal{T}}$ :

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$$Z_{\mathcal{T}}(\alpha_{\mathcal{T}}) \triangleq \left[ \phi(\Sigma_{\mathcal{T},1}, \bar{\Sigma}_{\mathcal{T}}, \alpha_{\mathcal{T}}), \dots, \phi(\Sigma_{\mathcal{T},1}, \bar{\Sigma}_{\mathcal{T}}, \alpha_{\mathcal{T}}) \right]^\top \in \mathbb{R}^{N_{\mathcal{T}} \times d(d+1)/2}$$

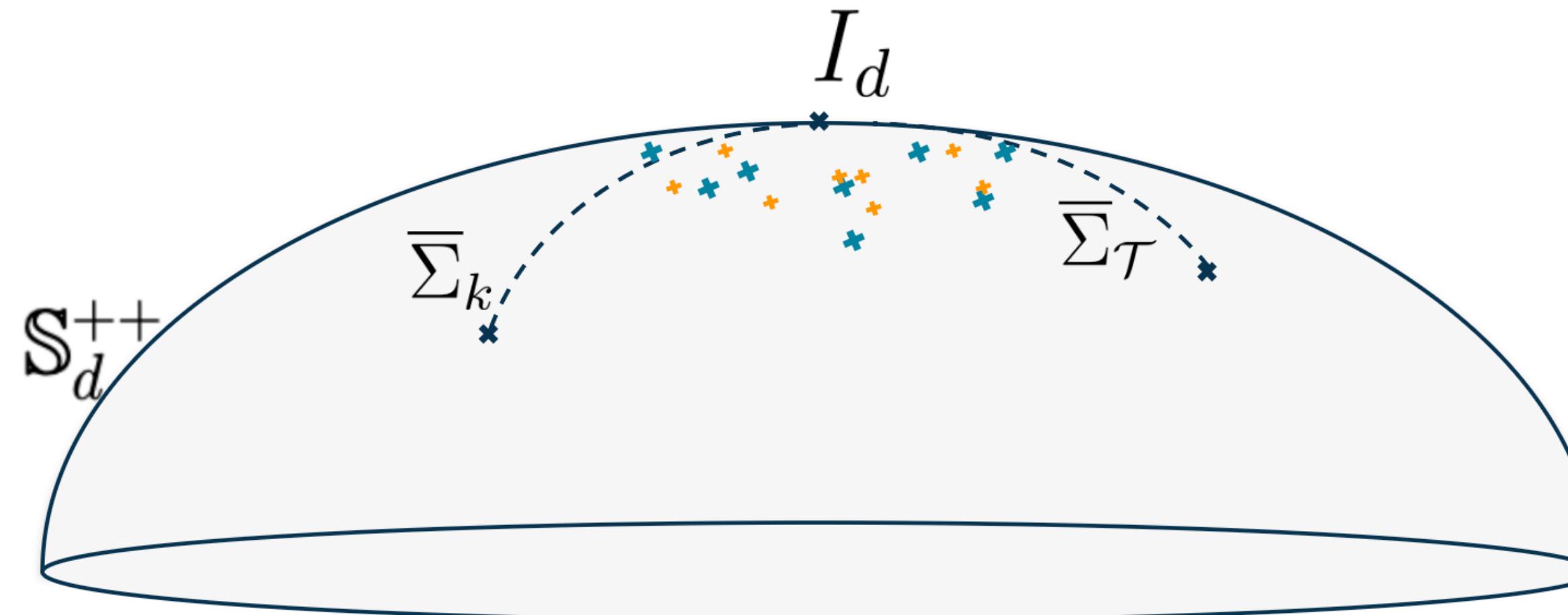


# GOPS: Geodesic Optimization for Predictive Shift Adaptation

Learnable source and target data matrices w.r.t.  $\alpha_{\mathcal{S}} \in [0,1]^K$  and  $\alpha_{\mathcal{T}}$ :

$$Z_{\mathcal{S}}(\alpha_{\mathcal{S}}) \triangleq \left[ \phi(\Sigma_{1,1}, \bar{\Sigma}_1, \alpha_1), \dots, \phi(\Sigma_{K,N_K}, \bar{\Sigma}_K, \alpha_K) \right]^\top \in \mathbb{R}^{N_{\mathcal{S}} \times d(d+1)/2}$$

$$Z_{\mathcal{T}}(\alpha_{\mathcal{T}}) \triangleq \left[ \phi(\Sigma_{\mathcal{T},1}, \bar{\Sigma}_{\mathcal{T}}, \alpha_{\mathcal{T}}), \dots, \phi(\Sigma_{\mathcal{T},1}, \bar{\Sigma}_{\mathcal{T}}, \alpha_{\mathcal{T}}) \right]^\top \in \mathbb{R}^{N_{\mathcal{T}} \times d(d+1)/2}$$



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Train-time:

$$\alpha_{\mathcal{S}}^* \triangleq \arg \min_{\alpha \in [0,1]^K} \| y_{\mathcal{S}} - Z_{\mathcal{S}}(\alpha) \beta_{\mathcal{S}}^*(\alpha) \|_2^2$$

subject to  $\beta_{\mathcal{S}}^*(\alpha)$  is the ridge estimator

Test-time:

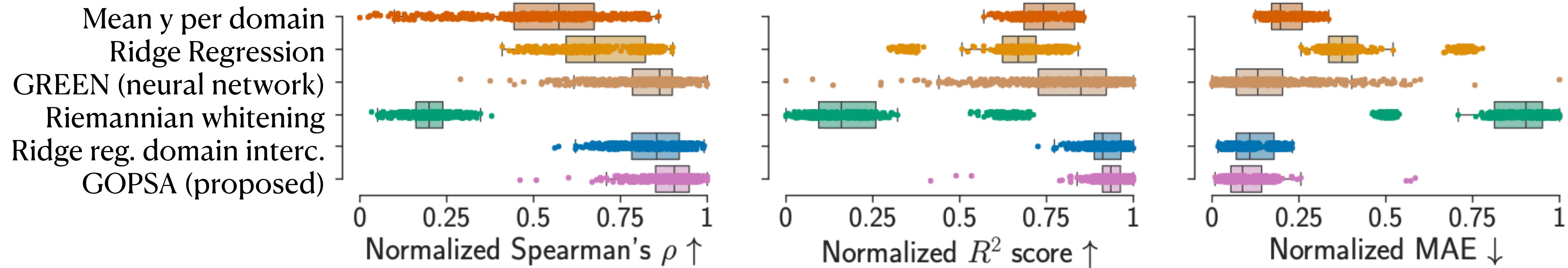
(Optimization)  $\alpha_{\mathcal{T}}^* \triangleq \arg \min_{\alpha \in [0,1]} \left( \bar{y}_{\mathcal{T}} - \text{mean} \left( Z_{\mathcal{T}}(\alpha) \beta_{\mathcal{S}}^*(\alpha_{\mathcal{S}}^*) \right) \right)^2$

(Prediction)  $\hat{y}_{\mathcal{T}} \triangleq Z_{\mathcal{T}}(\alpha_{\mathcal{T}}^*) \beta_{\mathcal{S}}^*(\alpha_{\mathcal{S}}^*)$

# Evaluation

HarMNqEEG dataset [Li et al., 2022]

14 recording sites, 1500 human participants, random combination of source sites, single random target site



# Conclusions

## Benchmarks matter

→ Skada-Bench provides the first cross-modal, realistically-validated UDA benchmark

## Back to basics: affine distribution alignment across domains

→ simple affine methods help reduce cross-domain error without labels

## Joint shifts in $(X, y)$ on manifolds

→ EEG data live on manifolds, yet we can design simple and efficient methods—such as GOPSA—that outperform more complex alternatives

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## **2. SKADA-Bench: Benchmarking Unsupervised Domain Adaptation Methods with Realistic Validation**

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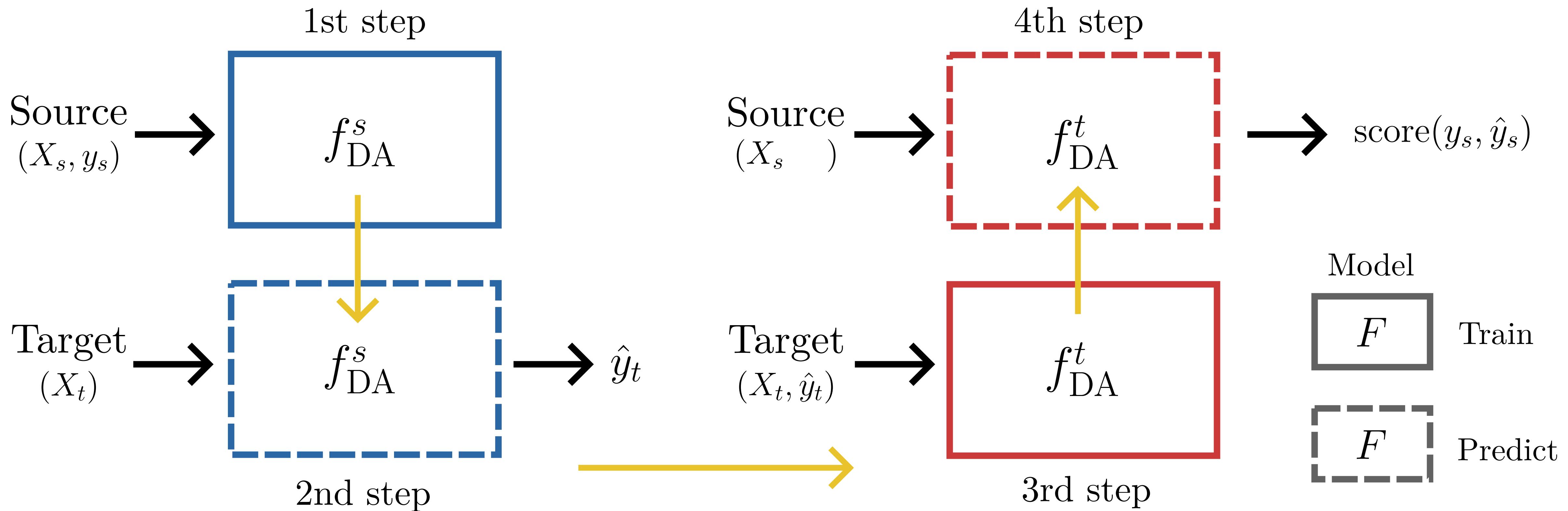
\*Equal contribution

<https://arxiv.org/abs/2407.11676>

# Datasets

<b>Dataset</b>	<b>Modality</b>	<b>Preprocessing</b>	<b>Pairs of Adaptation</b>	<b>Classes</b>	<b>Samples</b>	<b>Features</b>
Office 31	CV	Decaff + PCA	6	31	$470 \pm 350$	100
Office Home	CV	ResNet + PCA	12	65	$3897 \pm 850$	100
MNIST/USPS	CV	Vect + PCA	2	10	3000 / 10000	50
20 Newsgroup	NLP	LLM + PCA	6	2	$3728 \pm 174$	50
Amazon Review	NLP	LLM + PCA	12	4	2000	50
Mushrooms	Tabular	One Hot Encoding	2	2	$4062 \pm 546$	117
Phishing	Tabular	None	2	2	$5527 \pm 1734$	30
BCI	Biosignals	Cov + TS	9	4	288	253

# DA scorer: circular validation



# 3. Normalization for joint shifts in $(X, y)$ : GOPSA

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NeurIPS 2024, Spotlight

<https://arxiv.org/abs/2407.03878>

# GOPSA: Geodesic Optimization for Predictive Shift Adaptation

Setup:

$K$  source domains:  $\{(\Sigma_{k,n}, y_{k,n})\}_{n=1}^{N_k}$  for  $k \in \{1, \dots, K\}$  and  $N_{\mathcal{S}} = \sum_{k=1}^K N_k$

One target domain:  $\{\Sigma_{\mathcal{T},n}\}_{n=1}^{N_{\mathcal{T}}}, \bar{y}_{\mathcal{T}}$  (mean value)

Learn the parallel transport  $\alpha \in [0,1]$  per domain:

$$\phi(\Sigma, \bar{\Sigma}, \alpha) \triangleq \text{uvec} \left( \log_{I_d} (\text{PT}(\Sigma, \bar{\Sigma}, \alpha)) \right) = \text{uvec} \left( \log \left( \bar{\Sigma}^{-\alpha/2} \Sigma \bar{\Sigma}^{-\alpha/2} \right) \right)$$

# GOPS: Geodesic Optimization for Predictive Shift Adaptation

Train-time:

$$\alpha_{\mathcal{S}}^* \triangleq \arg \min_{\alpha \in [0,1]^K} \| y_{\mathcal{S}} - Z_{\mathcal{S}}(\alpha) \beta_{\mathcal{S}}^*(\alpha) \|_2^2$$

$$\text{subject to } \beta_{\mathcal{S}}^*(\alpha) \triangleq Z_{\mathcal{S}}(\alpha)^{\top} (\lambda I_N + Z_{\mathcal{S}}(\alpha) Z_{\mathcal{S}}(\alpha)^{\top})^{-1} y_{\mathcal{S}}$$

Test-time:

$$(\text{Optimization}) \quad \alpha_{\mathcal{T}}^* \triangleq \arg \min_{\alpha \in [0,1]} \left( \bar{y}_{\mathcal{T}} - \frac{1}{N_{\mathcal{T}}} \mathbf{1}_{N_{\mathcal{T}}}^{\top} Z_{\mathcal{T}}(\alpha) \beta_{\mathcal{S}}^*(\alpha_{\mathcal{S}}^*) \right)^2$$

$$(\text{Prediction}) \quad \hat{y}_{\mathcal{T}} \triangleq Z_{\mathcal{T}}(\alpha_{\mathcal{T}}^*) \beta_{\mathcal{S}}^*(\alpha_{\mathcal{S}}^*)$$

# GOPS: Geodesic Optimization for Predictive Shift Adaptation

Train-time:

$$\alpha_{\mathcal{S}}^* \triangleq \arg \min_{\alpha \in [0,1]^K} \| y_{\mathcal{S}} - Z_{\mathcal{S}}(\alpha) \beta_{\mathcal{S}}^*(\alpha) \|_2^2$$

$$\text{subject to } \beta_{\mathcal{S}}^*(\alpha) \triangleq Z_{\mathcal{S}}(\alpha)^{\top} (\lambda I_N + Z_{\mathcal{S}}(\alpha) Z_{\mathcal{S}}(\alpha)^{\top})^{-1} y_{\mathcal{S}}$$

Test-time:

Assumption:  $\bar{\Sigma}_{\mathcal{T}}, \bar{y}_{\mathcal{T}}$  are known

$$(\text{Optimization}) \quad \alpha_{\mathcal{T}}^* \triangleq \arg \min_{\alpha \in [0,1]} \left( \bar{y}_{\mathcal{T}} - \frac{1}{N_{\mathcal{T}}} \mathbf{1}_{N_{\mathcal{T}}}^{\top} Z_{\mathcal{T}}(\alpha) \beta_{\mathcal{S}}^*(\alpha_{\mathcal{S}}^*) \right)^2$$

$$(\text{Prediction}) \quad \hat{y}_{\mathcal{T}} \triangleq Z_{\mathcal{T}}(\alpha_{\mathcal{T}}^*) \beta_{\mathcal{S}}^*(\alpha_{\mathcal{S}}^*)$$